

## On the von Karman length scale as a triggering parameter in eddy-resolving simulations of turbulent flows

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The von Karman length scale ( $L_{vK} = \kappa S / |\nabla^2 U|$ ) represents a key element in triggering the flow to generate resolved turbulence in Scale-Adaptive Simulation (SAS, Menter and Egorov, 2010; *FTaC*, Vol. 85(1), pp. 113-138), analog to the role of grid spacing  $\Delta (= \sqrt[3]{\Delta_x \Delta_y \Delta_z})$  in Large-Eddy Simulation. Accordingly, the  $L_{vK}$  length scale mimics the length scale of resolved motion within the SAS framework, and the shear rate  $S (= \sqrt{2S_{ij}S_{ij}})$  represents its frequency scale. Jakirlic and Maduta (2015; *IJHFF*, Vol. 51, pp. 175-194) applied the SAS methodology to a near-wall Reynolds stress model, the  $\bar{u}_i \bar{u}_j$  model equation of which is coupled with the scale-supplying equation governing the homogeneous part of the inverse turbulent time scale ( $\omega_h = \varepsilon_h / k$ , with  $\varepsilon_h = \varepsilon - 0.5D_k^v$ ). The model capability to account for the vortex length and time scale dynamics is, in line with the SST-SAS model (Menter and Egorov, 2010), enabled through an additional term in the corresponding length-scale determining equation, providing selective enhancement of its production:

$$P_{SAS}^* = 2.3713 \kappa S^2 \left( \frac{L}{L_{vK}} \right)^{1/2} - 3C_{RSM,2} k \max \left( \frac{(\nabla \omega_h)^2}{\omega_h^2}, \frac{(\nabla k)^2}{k^2} \right)$$

The key issue here is the ratio of the turbulent length scale  $L = k^{1/2} / \omega_h$  to the von Karman length scale, formulated in terms of the second derivative of the velocity field ( $\nabla^2 U$ ). Generally, in accordance with its definition, the  $L_{vK}$  length scale exhibits different behavior under conditions of different flow straining (Figs. 1-3). Accordingly, it is not possible to unambiguously judge about the influence of the  $P_{SAS}^*$  term on the flow by analyzing the  $L_{vK}$  length scale only. It is just one parameter in a fairly extensive model formulation. Actually, the entire term  $S^2 (L/L_{vK})^{1/2}$  has to be analyzed. Nevertheless, in Figs. 1-3, showing the instantaneous field of the additional production term  $P_{SAS}^*$ , it is illustrated that in the regions with weak rate of strain, as in the flow core, the  $P_{SAS}^*$  term exhibits lower values compared to the immediate wall vicinity and highly unsteady separated shear layer regions characterized by intensified turbulence activity. It coincides clearly with the regions characterized by lower values of the ratio  $L_{vK} / \Delta$  ( $L_{vK} / \Delta < 1$ ). The full-length paper will give more detailed analysis about the structure of the  $P_{SAS}^*$  term as well as about its influence on the selective turbulence intensity enhancement contributing decisively to the improved prediction.

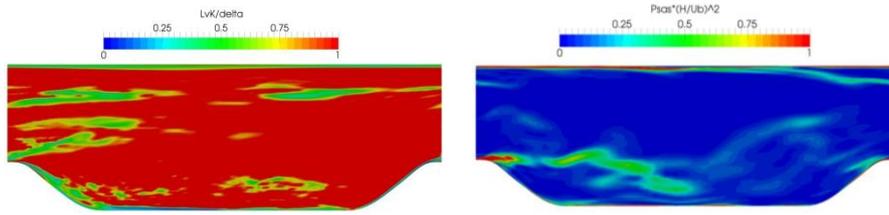


Figure 1: Flow over a 2D hill – iso contours of the  $L_{vK}$  length scale (normalized by grid spacing) and the  $P_{SAS}^c$  production terms

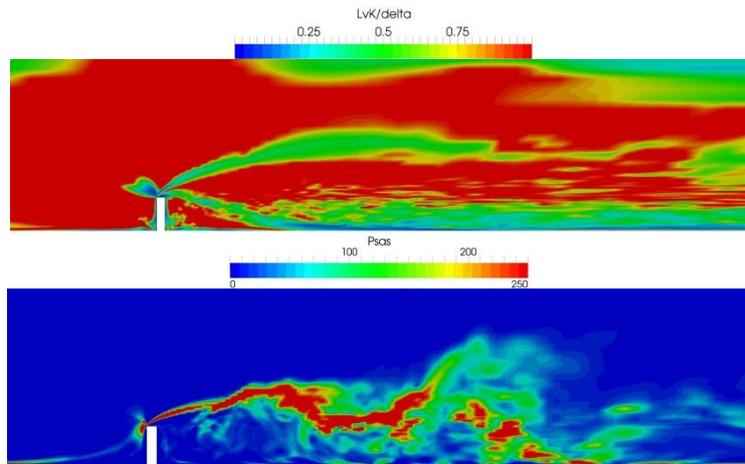


Figure 2: Flow over a 2D fence – iso contours of the  $L_{vK}$  length scale (normalized by grid spacing) and the  $P_{SAS}^c$  production terms

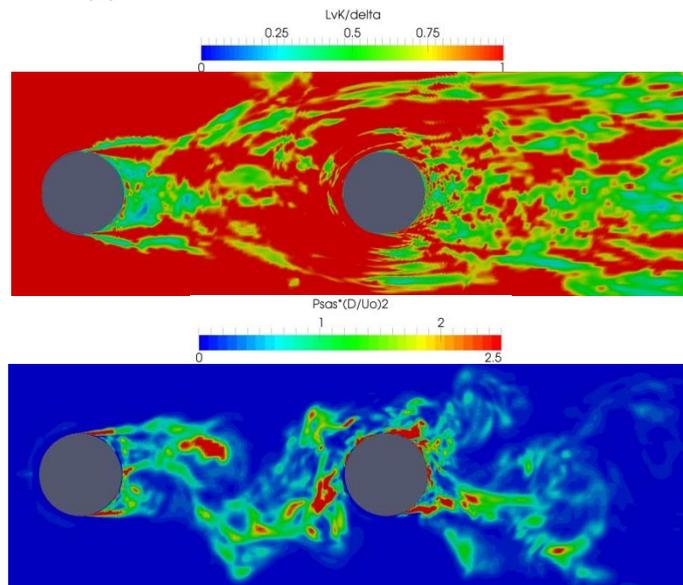


Figure 3: Flow past a 2D tandem cylinder – iso contours of the  $L_{vK}$  length scale (normalized by grid spacing) and the  $P_{SAS}^c$  production terms